## Notes on the back story of this letter:

I sent this 10-page letter to Richard Nelson shortly after the previous one. The date is quite probably wrong: it wasn't stated in the letter proper, the envelope is missing, and there's some evidence that suggests it was written significantly earlier than the alleged Sept., 1980 date.

That aside, the letter includes a number of my materials, all of them intended for publication in the PPC Calculator Journal, namely:
(1) $\boldsymbol{R F}$, a short but very capable \& fast general root finder routine for the HP-41C, which features an interactive prompting version ( $R F P$ ) as well as a non-prompting one ( $R P F$ ) callable from user's programs. Errors are automatically avoided if the derivative happens to be 0 , as are infinite loops in case of non-real roots or nonconvergence. This routine was submitted for its inclusion in the PPC ROM (only 83 bytes) and of course it didn't make it.
(2) A Chess playing program for the HP-67 which allows the user to play chess vs. the HP-67. The user conducts the Black king vs. the whole White army conducted by the HP-67. If the program manages to give checkmate in 6 moves or less, it wins; else, the user wins (being stalemated is also a win for the user).
(3) T, a revision of the Arithmetic Teacher program featured in the Standard Applications Pac included with every HP-41C. My revision works the same as the original but it's 120 lines/32 registers (vs. 163/52) so it saves as many as 20 registers for other uses and fits in a single mag card. I naively expected the programs in the Standard Pac to be optimized examples demonstrating efficient programming techniques but it seems I was wrong.
(4) Inputs to the FEEDBACK, 41C NOTES and/or ROUTINES sections, including my various optimizations and corrections to routines proposed for the PPC ROM by diverse authors, e.g.: to Improved Synthetic Key Assignments by Tom Cadwallader, or to a routine by William C. Wickes which I discovered it gave erroneous results for a range of arguments.
(5) A PROGRAMMING TIP showing in full detail how to very easily create on the fly a program line containing any arbitrary text (synthetic characters and all) using just STO band RCL b, no CODE or similar cumbersome programs needed. A full example is given.

Finally, I comment on the proposed inclusion in the $P P C$ ROM of a multi-function plotting program by Jake Schwartz that would take some 987 bytes, i.e. about $25 \%$ of the ROM.

Dear Richard:
I cannot resist the temptation of writing another submittal to the PPC Joumal. It must be some kind of PPCmania, you know; as soon as $I$ have some free time, I spend most of it writing something for its publication in my beloved PPCJ, although I know you'd never published anything contributed by poor Spanish member 4747 (that's me). Well, now seriously, here included are :

> -several inputs for the columns "FEEDBACK", " 410 NOTES", "IIPS"
> -one input for the PPC Custom ROM : a very short \& fast root finder
> -one $67 / 97$ program: A CHESS PLAYING PROGRAM

The root finder routine is included recorded on a magnetic card. The 67/97 program is not, as I have no 67/97 to record it, and a 410 version will not work on an actual 67/97. Several comments about the routines included:

- the programming tip shows how to synthesize any text, composed of any characters as a line in a program, making use of just STO b, RCL $b$, in a bugless machine. NO "CODE", "DECODE" programs, no bugs, just STO b, RCL b. This is a part of a future article regarding the properties \& applications of STO, RCL b. The article (to be contributed in the future) shows also how to break PRTVATE using only STO, RCL b, as I told you in my previous letter.
- the SYNTHETIC KEY ASSIGNMENTS program, which you think may be included in the PPC Custom RON may be greatly improved. Here included is a simple modification that saves 19 bytes at no cost, and quite a lot of initialization time. If the WSTS option is deleted (see the reasons), another 12 bytes are saved. I have now a totally different version of this program that combines all the properties of "CODE", "DECODE", "UNBLD", "REBLD" (Wickes) \& "SYNTHETIC KEY ASSIGNMENTS" (Cadwallader) onto' a single magnetic card, thus being much shorter, and certainly faster. However, the version is not complete to the moment, as I find a little inconvenient to look up CTAL-HEXADECDMAL conversion tables, because all inputs/outputs to my version are octal numbers, rather than decimal or hexadecimal values.
- the input for the PPC Custom RCM is a numerical root finder. I think that such a routine is needed in many applications (math, engineering, finance, etc.) and so I have worked out a suitable one. I have carefully read the articie on the HP JOURNAL about the solve key and decided to provide a method which, being very short (to avoid taking up excessive space in the Custom ROM) has most advantages of SOLVE, and it is nearly double fast. I didn't try to write a very convolute routine but a short, fast, general purpose one, as I think all routines included in the PPC Custom RCM should be. Despite its simplicity you'll find harder to beat its speed and efficiency. Try the given examples.
-the 67/97 program is my response to Joseph O. Holmes (3673), who asked for more 67/97 material, specially "non-mastermind" type programs. This one plays chess, and it is very hard to beat.
Only a final comment re: MUITI-FUNCTION PLOTPING by Jake Schwartz (V7 N1 P29)
Jake suggests the possibility of including its multi-function plotting in the Custom ROM. I disagree. Consider that most PPC members don't own a printer. What should they have to do with this program? . Of course, PPC members who have a printer deserve some attention, but this program is about 987 bytes long, this is almost 1 K of memory ! It is too much ! And, do you think that it is very useful to plot more than 3 curves at onoe ? Besides, the progrem is very slow. It takes a lot of time to work. Please, don't take these lines as a hard criticism to the program, I can't do it batter, I only express my opinion that taking up IK of memory of the PPC Custom ROM to include a program only useful to those members with a printer, and which also need to plot 3 or more functions at once, and they need to do it at maximum resolution, even if it takes 2 days to do it, is quite a specialized application, don't you believe? Please, stop joking and look for short (or long) general purpose routines which are useful to all members
- this is an input to your column "41c NOTES"

REVISION OF ARTMMETIC TEACHER PROGRAM, HP-41c STANDARD APP.
Here is an improved version of the pragram "Arithmetic Teacher" included in the Standard Applications Pac. The program runs following the same guidelines, only the initial seed is previously stored in ROO, and the name of the program is " T "


COMMENTS: The program has been reduced from 163 lines (52 registers) to 120 lines ( 32 registers), thus as many as 20 registers of program memory are saved. In ite present format the pragram exactly fits onto 1 magnetic card, so key it in exactly as it's written. A single byte added makes it neccessary to use a second mag card. Let the final END of program memory be the END of the program. SIZE is reduced from 010 to 008. The specifications are the same as the previous ones, except some prompting sounds have been changed. The tune played is exactly the same, the seed should be stored previously in ROO, and the name of the program is changed to "T". Happy programming.
-the following are some inputs to "FEEDBACK" or "41c -
NOTES" or "ROUTINES", I am not very sure in fact...

-     -         -             -                 -                     -                         -                             -                                 -                                     -                                         -                                             -                                                 - 

Reference: HIGH RESOLUTION PLOPTING by Nathan Meyers (4795) see V7 N2 pp. 49-50
-steps 101, 103, 105, 107, 109, 111 can be changed to ST+ X all of them ; this saves 12 bytes and speeds up the process.
-the 11.017 at lines 53, 134, 152 may be stored in an unused register at the beginning, and recalled at proper times. This would save at least 6 bytes, and muns faster as well.

VaLENTIN ALBILLO (4747)

Reference: SYNPHETIC FUNCTION ROUTINES by Bill C. Hickes see V7 N3 pp.6-7
-the routine "MANT" does not work properly for an arbitrary number. In fact, most numbers $X$ less than 1 give erroneous results.

For instance, for $x=F R C(P I)$ "MANT" gives 1.4159265-00, (it should be .141592654), which can t be used in most subsequent computations because of its -100 exponent.

VAIENTIN ALBILLO (4747)

Reference: IMPROVED SYNTHETIC KEY ASSIGNMENTS program by Tom Cadwallader (3502). See V7N3P3
-Iines 13 to 22 (both included) may be shortened to a single text line: it should be a text composed of the following 5 characters:

| - full man | (HEX 01, DEC 01) |
| :---: | :---: |
| - box star | (HEX 69, DEC 105) |
| - "mu" | (HEX $\propto$, DEC 12) |
| - null | (HEX 00, DEC 00) |
| - box star | (HEX BF, DEC 191) |

this text is easily created, and once it is synthesized as a line in the program, it saves 19 bytes (almost 3 res) and saves much time of initialization (in fact, 5 sub routine calls to LBI A are avoided).
-LBL C , the "write status option", should be deleted. I don't think it is efficient to waste 12 bytes in the PPC Custom ROM in a function that is already in the Card Reader ROM, and that may be assigned to a key for execution.
-further refinements are possible. I will submit a much shorter version of this program very soon (I hope).
VAIENTIN ALBILLO (4747)

PROGRAMMING TIP: Do you want to create an arbitrary text as a line in your program ? Follow this example: (You-ll need only RCD b, STO b assigned to keys)

Let us create the program line 05 , which is to be a text of the following 5 characters:

- full man (HEX 01), box star (HEX 69), "mu" (HEX $\infty$ ), null (HEX 0 ), box star (HEX BF)

18) In the desired line enter a normal text of the same number of characters as the text you wanto to create: O5 "ABCDE"
19) BST, press SIN , ST + IND 18
20) PACK
21) position yourself at the ST+ IND 18 , switch to RUN mode (if you followed (20) and (30) strictly, you already were at line ST+ IND 18, of course)
22) RCL b, go out of USER mode
23) switch to PRGM, BST, (you should see SIN), delete the SII
24) PACK , switch to RUN mode
25) STO b , switch to PRGM mode. You should see something like ST+ IND M (as it's the case in this example)
26) Looking at the HEX TABIE (V6 N5 P-22,23), key into program memory the keys whose HEX codes are the same as the characters you want to create:

$$
\begin{aligned}
\text {-in this example: full man } & =\text { LBL } \infty \\
\text { box star } & =\text { FRC } \\
\text { "mu" } & =\text { LBL } 11 \\
\text { ("mull", a littie problem) "mu" } & =\text { IBL } 11 \\
\text { box star } & =\text { GTO } 14
\end{aligned}
$$

so, key in (you are at line ST+ IND M) : (first, go out of USER mode, of course): LBL OO, FRC, LBL 11, LBL 11, GTO 14
108) In this example, the 4 th character was a null. To simplify the process, the null was introduced as another "mu". Now, to create the null:
-switch to RUN mode, STO b, (yOu should see ag

$$
\text { the } \mathrm{cm} \text {. } 0 \text { oc } \mathrm{com} \mathrm{~cm} \mathrm{cam} 1
$$

the ST + IND M) ; SST, SST, SST, SST (y ou should see the second LBL 11). Delete the IBL 11 you are seeing. Delete the ST + IND 18 you are seeing now. SST and you should see your synthesized line.
110) Delete the (in this example) 5 lines after your text: they are the $A, B, C, D, E$ of the original text.
122) Your text is created. Be careful not to make a mistake during the whole process. Remember, nulls are introduced as any single-byte instruction which is doleted later.

Simple, isn`it ? Only STO b, RCL b, no CODE, no DECODE, no bug, no nothing.

VALENTIN AIBILLO (4747)

- the following is an input to your column "ROM PROGRESS"

After many years of owning several HP's programmable calculators, ( $\mathrm{HP}-25, \mathrm{HP}-67 \& \mathrm{HP}-41 \mathrm{C})$, I have realized that several kind of subroutines appear very frequently enclosed into the body of another main program.

One of this frequent routines is a root finder program: it finds the roots (one root at a time) of a general equation $f(x)=0$. It appears in :

- mathematical problems: solve $f(x)=0$ (of course!)
- engineering: gear wheels ( $\tan x-x=I)$
- chemical problems: weak acid-base titrations
- financial problems: find IRR of an investment
and many others. This need is recognized even by HP: the new handheld calculator $\mathrm{HP}-34 \mathrm{c}$ includes a numerical root finder, SOLVE, among its built-in capabilities.

All this makes me think that a numerical root finder method should be implemented into the PPC Custom ROM . This would render all problems mentioned before to be considered as trivial programs. See examples. Now, what kind of numerical root finder ? Anyone who believes that root finding is easy, should read the article 'Perso nal calculator has key to solve any equation $f(x)=0^{\prime \prime}$, published in the HP JOURNAL, December 1979, pp-20. This article gives an idea of the kind of troubles one gets into when trying to program a "foolproof" root finder.

After careful thought, I decided that a soft ware version of the hardware SOLVE function on the 34 c , would not be very efficient: the SOLVE function is almost foolproof, it takes many attention to the resources neccessary to cope with bad guesses, unconvenient $f(x)$, noise error, etc, resulting in not very fast execution times. Besides, SOLVE alweys finds the root to 10 significant pla ces, but most real world applications are exact to 2 or 3 places only, and finding to 10 places a root of an equa tion whose numerical coefficients are reliable to 2 places is a waste of time, to say the least.

Taking all this into consideration, I decided to present the following numerical root finder for its inclu sion into the PPC Custom ROM:

| 01 LBL "RF" | 1250 | 23 XEQ IND $\varnothing \varnothing$ | 34 RND |
| :---: | :---: | :---: | :---: |
| 02 "NAME?" | 13 STO 0 | $24 \mathrm{X}=\varnothing$ ? | $35 \mathrm{X}=\varnothing$ ? |
| 03 AON | 14 LEL $\varnothing \varnothing$ | $25 \mathrm{GTO} \emptyset_{1}$ | 36 OTO $\varnothing_{1}$ |
| 04 PROMPT | 15 RCL N | 26 ST-M | 37 DSE 0 |
| 05 AOFF | 161 | 27 RCL M | 38 GTO ¢D |
| 06 ASPO $\varnothing \varnothing$ | 17 D -R | $28 \mathrm{X}=\boldsymbol{\phi}$ ? | 39 SF $\varnothing \varnothing$ |
| 07 "xpa?" | $18 \mathrm{D}-\mathrm{R}$ | 29 SIGN | $40 \mathrm{LBL} \phi_{1}$ |
| 08 PROMPT | $19+$ | $30 /$ | 41 RCL N |
| 09 LBL "RFP" | 20 XEQ IND $\phi \varnothing$ | 31 D-R | 42 CLA |
| 10 CF ¢ $\varnothing$ | 21 STOM | $32 \mathrm{D}-\mathrm{R}$ | 43 END |
| 11 STO N | 22 RCL N | 33 ST-N |  |

The program is 43 lines long, only 83 bytes. It requires SIZE OO1, and uses synthetic functions STO M,N,O,RCL M, RCL N, ST-M,N, DSE 0 . The registers $M, N, O$ are used as mere auxiliars, to help save 3 registers. If synthetic functions are not tolerated, $M, N, O$ should be changed to $\phi 1, \phi 2, \phi 3$ respectively. This increases size to SIZE 004, the line 42 CLA should be deleted, and 8 bytes would be saved. The routine uses flag $\varnothing$ and doesn't alter the angular mode, fix display or whatever except the alpha register, which is used, then cleared.

It is based in the well-known Newton's method:

$$
x_{n+1}=x_{n}-f\left(x_{n}\right) / f^{\prime}\left(x_{n}\right)
$$

where the derivative $f^{\prime}\left(x_{n}\right)$ is computed as
$f^{\prime}\left(x_{n}\right)=\left(f\left(x_{n}+k\right)-f\left(x_{n}\right)\right) / k$, where $k=3 E-4$
Thus, the method requires only 2 evaluations of $f(x)$ per iteration, and its rate of convergence is quadratic: the number of exact places almost doubles on every iteration. The program is written so to be short and fast: it is faster than SOLVE in most cases. The speed depends most on your $f(x)$. Two versions are provided: (both in the same p)
-interactive version : call "RF", and the program will prompt for the name of your function, and the initial guess, $x_{0}$, for the root, then proceed to compute the root and stop with the root in the display.
-prosrammable version : call "RFP", which assumes that the NAME of your function is in register 00 , the initial guess, $X \phi$, is in the display. Then computes the root and returns it to the $X$ register.
WARNINGS: - if $y^{\circ}=0$, the program takes $y^{\prime}=1$, then resumes the execution. This results in that a local minimum or maximum will give no trouble: it will get out of there in most cases.

- the program will periorm up to 50 iterations. If the root is found within this limit, it will be presented, and the flag 00 will be cleared. If it is not found to the desired accuracy within 50 loops, the best approximation should be displayed, and flag 00 will be set. This avoids a forever running. You should test flag $\overline{00}$ to see if it is set or clear after the program returns to your main program, and decide What to do (maybe the root displayed needs a little refine ment, or maybe the equation has no roots in that zone). This simulates the conditional property of SOLVE.
- the accuracy depends on the FIX $n$ display. The greater $n$, the better the accuracy. Most times the computed root will be more accurate than it seems. If you need 2 or 3 places only, set FLX 2. If you need full accuracy, set FIX 7. Of course, more accuracy requires more time to achieve.
- after the execution, NAME remains unaltered in register 0, and alpha register is cleared.

EXAMPLES : using FIX 7 in all of them:
$e^{x}-5 x+3=0 ; X_{0}=1$ gives $1.4688293(12$ seconds)
$X_{0}=2$ gives $1.7437520(12$ seconds)
(they are nearby roots and are correct to 9 places)
$x^{2}-4 x+4=0 ; X_{0}=1$ gives 1.9999908 ( 21 seconds)
(it is a double root, $x=2 ; f(1.9999908)$ is zero to 10 ples) $x^{2}+1=0 ; X_{0}=0$ gives -3.3380759 and flag 00 is set
(after 50 iterations no root was found ; flag 0 is set, and the last iterated is presented; there are no real roots)
$\theta^{\pi}-2=0 ; X_{0}=1$ gives 0.6931472 in 8 secands Xo $=20$ gives 0.6931472 in 40 seconds Xo $=90$ gives 40.0080372 and flag $\infty$ is set ; the root was not found after 50 iterations, because the initial guess was very far from the root, and the EXP (x) is very sharp. However, XBQ"RFP" will give now 0.6931472 starting from the 40.0080372. Be a littie careful with your Xo.

VAIENTIN ALBILLO (4747)
P.S.: remember, this program is very short, but it should help in most cases. I could write a very cumbersome program which will take into aocount very special cases, but the RCM should have only general purpose routines, not complete courses on numerical analysis or whatever.

I totally agree with Joseph O. Holmes (3673) about the need for 67/97 programs. Not everyone in this Club owns a 41c. I HAVE a 41c (and a card reader, 3 modules, several pacs, etc ), but I don't think that is good for the Club to dedicate all of its efforts to the new gadget. If PPC should grow, it should maintain its present membership as well, and it's quite possible to lose many members which don't find support for their models and don't understand either the many complexities of the 41c. So, please, stop a little with the repetitions of 41 c material (for instance, article "MORE TONES" in V7 N3 P26 is almost a duplication of previous articles) and start with new and fresh 67/97, 34c, 33 materials.

This game program will allow you to play chess against any HP-67/97. Here the calculator plays the 16 white pieces, and you have only the black king. The initial position is the standard one given below. Calcula-
 tor will try to play and checkmate in 6 moves or less: if it succeeds, it will be considered the winner. Of cour se, your goal is to play in such a way as to make a checkmate within 6 moves (or less) impossible. Also, you can try to force a stalemated position this is, a position in which you are neither in check nor able to make any legal move; in that case, you will be considered the winner too.

GAME CONVENTIONS : a) WHITE (HP): output of white's moves is performed accordingly to the following convention:

| PIECE | CODE | PIECE | CODE |
| :---: | :---: | :---: | :---: |
| king, K | 6 | bishop, B | 3 |
| queen, Q | 5 | knight , Kt | 2 |
| rook , R | 4 | pawn , P | 1 |

Output is of the form XYZ.N, where:
$-X=$ code of the piece White has just moved
$-Y=$ code of the piece in whose colum lays now the moved piece (up to 2 digitss the first one then specifies if it is a king side or queen side pieoe)
$-Z=$ indicates in which square of the column rest the moved pieoe, counting upwards from the bottom.
$-\mathrm{N}=$ Number of White's moves already performed.
Examples: should White move a pawn to King's bishop 4 on its second move, the output would be: 1634.2 ( $=\mathrm{P}-\mathrm{KB4}$ on the 2nd move)
if the output were 5627.4, this would be decoded so:
$5=$ stands for queen, $Q$
$62 \times 6$ stands for King, $K$, and 2 for Knight, Kt
$7=$ the 7 th square of the column
$4=$ the 4 th move of White.
so, this means that White plays its queen (5) to the 7 th square (7) of its King (6) side knight (2) column on its 4 th (4) move.
All in all, there are 3 kinds of output:
normal $=X Y Z . N$, in DSP 1
check $=-X Y Z . N$, in DSP 1
checkmate $=-X Y Z .00000$, in DSP 9
b) BLACK: your moves are input in quite a different way; to move your black king, you must input the XY coordinates of the square it moves to, following the

$X-Y$ notation indicated in the figure. For instance, in the initial position your king is in 58. To move your king to the location indicated by the arrow, you must input: $47 \mathrm{R} / \mathrm{S}$
If your king takes a white piece on its move, the procedure is the same as before, but you must change the sign of your input. To take the pawn in the figure, input $-53 \mathrm{R} / \mathrm{S}$. To run the program, you will need to have the following data stored: (make a data card with them)

| P.regis : | 0 | 1 | 2 |  | 3 |  | 4 |  | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| contents: | 164 | 524 | 527 |  | 154 |  | 557 |  | 525 | 3634 | 537 | 155 | 336 |
| P.regis : | A | B | C |  | D | D | E |  | I |  |  |  |  |
| contents: | 1523 | 322 | 33 | 34 | 10 |  | 0.8 |  | 0 |  |  |  |  |
| S.regis 8 | 0 |  |  | 2 |  | 3 |  | 4 | 5 | 6 | 7 | 8 |  |
| contents: | 3525 | 55 |  | 565 |  | 325 |  | 0 | 346 | 3534 | 567 | 562 |  |
| Soregis : <br> contents: | $\frac{9}{353}$ | -This data card is needed only when loading the program. |  |  |  |  |  |  |  |  |  |  |  |

HARNINGS : illegal moves of yourself can't be corrected, and a re-start would be needed.
-program does not always indicate check status. These situations are infrequent, however.

INSTRUCTIONS : load program card \& data card

1) start the game: press A $\rightarrow$ White's first move
2) input your answers $X Y R / S \rightarrow$ White's and move repeat (2) until HP checkmates you. If you roach the move number 6 without being checkmated, you have won. If HP checkmates you on its 6th move (or less), HP has won.
3) for another game, go to (1)

EXAMPIE: let‘s have a game. I'll play as bad as possible:
$A \rightarrow 164.1(=P-K 4)$, I move to $68: 68 \mathrm{R} / \mathrm{S} \rightarrow 524.2(=Q-K t 4)$
$67 \mathrm{R} / \mathrm{S}>557.3(=Q-\mathrm{Q7})$
$68 \mathrm{R} / \mathrm{S} \rightarrow 1523.4\left(=\mathrm{P}-\mathrm{QK}_{\mathrm{K}} \mathrm{H} 3\right)$
$78 \mathrm{R} / \mathrm{S} \rightarrow-334.5(=\mathrm{B}-\mathrm{B4})$
A check !
$68 \mathrm{R} / \mathrm{S} \rightarrow-322.0000006$
this is, $\mathrm{B}-\mathrm{K} \mathrm{t} 2$.
Checkmate • I'VE LOST

- This is finished. HP has checkmated my king on its 6th move, so I have lost. I played very badly. Perhaps you will do better.

| 001 LBL A | 312511 | 051 CHS | 42 | 101 P ()S | 3142 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 022 DSP 1 | 2301 | 052 GSB 2 | 312202 | 102 RCL 5 | 3405 |
| 0030 | $\infty$ | 0535 | 05 | 103 P () S | 3142 |
| 004 ST I | 3533 | 0546 | 06 | 104 GTO 3 | 2203 |
| 005 RCL 0 | 3400 | $055 \mathrm{X} \neq \mathrm{Y}$ | 3261 | 105 LBL 0 | 312500 |
| 006 GSB 2 | 312202 | 056 GTO 5 | 2205 | 106 GSB 6 | 312206 |
| 007 RCL 1 | 3401 | 057 RCL 8 | 3408 | $107 \mathrm{X}=\mathrm{Y}$ | 3261 |
| 008 GSB 7 | 312207 | 058 GTO 9 | 2209 | 108 GTO 4 | 2204 |
| 009 NNT | 3183 | 059 LBL 0 | 312500 | 109 RCL 9 | 3409 |
| 0106 | 06 | 060 CSB 6 | 312206 | 110 GSB 2 | 312202 |
| $011 \mathrm{X}=\mathrm{Y}$ | 3251 | 061 X $\ddagger$ Y | 3261 | 1112 | 02 |
| 012 GTO C | 2213 | 062 GTO 0 | 2200 | 1128 | 08 |
| 013 RCL 2 | 3402 | 063 P ()S | 3142 | $113 \mathrm{X} \neq \mathrm{Y}$ | 3261 |
| 014 GSB 7 | 312207 | 064 RCL 0 | 3400 | 114 GTO 4 | 2204 |
| 015 Frac | 3283 | 065 P() S | 3142 | 115 RCL 2 | 3402 |
| 016 RCL E | 3415 | 066 GSB 2 | 312202 | 116 GTO 9 | 2209 |
| $017 \mathrm{X}=\mathrm{Y}$ | 3251 | 067 LBL 4 | 312504 | 117 LBL C | 312513 |
| 018 GTO D | 2214 | $068 \widehat{\text { RCL } 4}$ | 3404 | 118 RCL 4 | 3404 |
| 019 RCL 3 | 3403 | 069 GTO 9 | 2209 | 119 GSB 7 | 312207 |
| 020 GSB 2 | 312202 | 070 LBL 0 | 312500 | 120 FRAC | 3283 |
| 0212 | 02 | 071 Rdown | 3553 | 121 RCL E | 3415 |
| 0226 | 06 | 0721 | 01 | $122 \mathrm{X}=\mathrm{Y}$ | 3251 |
| $023 \mathrm{X} \neq \mathrm{Y}$ | 3261 | 0735 | 05 | 123 GTO B | 2212 |
| 024 GTO 0 | 2200 | $074 \mathrm{X} \neq \mathrm{Y}$ | 3261 | 124 RCL 3 | 3403 |
| 025 RCL 4 | 3404 | 075 GTO 0 | 2200 | 125 GSB 2 | 312202 |
| 026 LBL 8 | 312508 | 076 P () S | 3142 | 1266 | 06 |
| 027 GSB 2 | 312202 | 077 RCL 1 | 3401 | 1276 | 06 |
| 028 RCL 5 | 3405 | 078 F() S | 3142 | 128 Xfy | 3261 |
| 029 LBL 9 | 312509 | 079 GTO 8 | 2208 | 129 GTO 0 | 2200 |
| 030 CHS | 42 | 080 LBL 0 | 312500 | 130 P () S | 3142 |
| 031 DSP 9 | 2309 | $081 \overline{\mathrm{P}}$ ()S | 3142 | 131 RCL 6 | 3406 |
| 032 ISZ | 3134 | 082 RCL 2 | 3402 | $132 \mathrm{P}($ ) S | 3142 |
| 033 RC I | 3534 | 083 P() S | 3142 | 133 GS3 2 | 312202 |
| 034 EEX | 43 | 084 GTO 8 | 2208 | 134 LBL 5 | $31 \quad 2505$ |
| 0357 | 07 | 085 LBL D | 312514 | 135 RCI 7 | 3407 |
| 036 / | 81 | 086 P()S | 3142 | 136 GTO 9 | 2209 |
| $037-$ | 51 | 087 RCL 3 | 3403 | 137 LBL O | 312500 |
| 038 RTN | 3522 | 088 P() S | 3142 | $138 \overline{\text { GSB } 6}$ | 312206 |
| 039 IBL O | 312500 | 089 GSB 2 | 312202 | $139 \mathrm{X} \neq \mathrm{Y}$ | 3261 |
| 040 CSB 6 | 312205 | 0901 | 01 | 140 GTO 0 | 2200 |
| $0.41 \mathrm{X} / \mathrm{Y}$ | 3261 | 0918 | 08 | 141 P()S |  |
| 042 Gro 0 | 22 0 | $092 \mathrm{X} \neq \mathrm{Y}$ | 3261 | 142 RCL 7 | 3407 |
| 043 RCL 6 | 3406 | 093 GTO 0 | 2200 | 143 P() S | 3142 |
| 044 GSB 2 | 312202 | 094 RCL 9 | 3409 | 144 GIO 8 | 2208 |
| 045 GTO 5 | 2205 | 095 CHS | 42 | 145 IBL 0 | 312500 |
| 046 IBL 0 | 312500 | 096 GTO 3 | 2203 | 146 Rdown | 3553 |
| $047 \overline{\text { GSB } 6}$ | 3122 on | 097 IBL 0 | 312500 | 147 X)0 | 3181 |
| $048 \mathrm{X} \neq \mathrm{Y}$ | 3261 | 098 GSB 6 | 3122 os | 148 GTO 0 | 2200 |
| 049 Gro 0 | $22 \times$ | $099 \mathrm{X} \neq \mathrm{Y}$ | 3261 | 149 P() S | 3142 |
| 050 RCL 6 | 3406 | 100 GTO 0 | 2200 | 150 RCL 9 | 3409 |



